

1. **a.** Let  $b$  stand for the base of  $f(x)$ . Then  $f(5) = b^3 \cdot f(2)$ , and  $f(8) = b^3 \cdot f(5)$ .  
Substitute the given information into the first equation to get  $b^3 = k/4$ .  
Then the second equation gives  $f(8) = (k/4) \cdot k = k^2/4$ .
- b.** From part **a**,  $b^3 = k/4$ , so  $b = \sqrt[3]{k/4}$ . So the model is  $f(x) = a \cdot (\sqrt[3]{k/4})^x$ , and there remains only to find  $a$ . To do so, substitute the given point  $f(2) = 4$ , and solve for  $a$ :

$$4 = a \cdot (\sqrt[3]{k/4})^2$$
$$a = \frac{4}{(\sqrt[3]{k/4})^2}$$

So the final answer is:

$$f(x) = \frac{4}{(\sqrt[3]{k/4})^2} \cdot (\sqrt[3]{k/4})^x \quad \text{or more simply } f(x) = 4(k/4)^{\frac{x-2}{3}}.$$

2. Set  $n \cdot e^{-0.0001216 t} = \frac{n}{2}$ . Simplify by dividing by  $n$ , which gives  $e^{-0.0001216 t} = \frac{1}{2}$ .  
Solve the equation graphically on your calculator to get  $t \approx 5700$  years.
3. Your answer could be anything of the form  $g(t) = a \cdot 3^{\frac{t}{2}}$  or  $g(t) = a \cdot (\sqrt{3})^t$ .  
You may have chosen a specific number for  $a$ ; easiest is  $a = 1$ .
4. **a.** The range is  $20 \leq t < 200$ . If you thought the minimum was 0, note that  $P(0) = 20$ .
- b.** The maximum population is 200; 90% would be 180.  
Solve  $180 = \frac{200}{1 + 9e^{(-0.1)t}}$  graphically on your calculator to get  $t \approx 43.94$  years.